

Date 4/8/21

Test - 1

Qns: 1 (a) (i) Pressure = Energy per unit volume

(b) dimensional formula of angle is $M^0 L^0 T^0$
and S.I. unit is radian.

(c) Given,

$$F = kv^2$$

$$\begin{aligned}\therefore [k] &= \frac{[F]}{[v]^2} = \frac{M^1 L^1 T^{-2}}{[LT^{-1}]^2} \\ &= \frac{M^1 L^1 T^{-2}}{M^0 L^2 T^{-2}} = [M^1 L^{-1}]\end{aligned}$$

(d) we know,
density = mass / volume

$$= \frac{5.74}{1.2}$$

$$= 4.783 \text{ g/cm}^3$$

\therefore density = 4.8 g/cm^3 since least
count significant figure is 2.

Qns: 2 Given,

$$v^2 = u^2 + 2as$$

$\therefore [v] = [u]$ are velocities.

$$\text{i.e.} = [M^0 L^0 T^{-1}]$$

$$[a] = [M^0 L^1 T^{-2}]$$

acceleration = $[a] = [M^0 L^1 T^{-2}]$
 distance = $[s] = [M^0 L^1 T^0]$

$$L.H.S = [v]^2 = [M^0 L^1 T^{-1}]^2$$

$$= [M^0 L^2 T^{-2}] \quad \text{--- (I)}$$

$$R.H.S = [u]^2 + [2as] = [M^0 L^1 T^{-1}]^2 + [M^0 L^1 T^{-2}] [M^0 L^1 T^0]$$

$$= [M^0 L^2 T^{-2}] + [M^0 L^2 T^{-2}]$$

$$= [M^0 L^2 T^{-2}] \quad \text{--- (II)}$$

From (I) and (II), we get

$$R.H.S = L.H.S$$

Hence, the equation is correct.

(b) Given,

$$\left(p + \frac{a}{v^2} \right) (v-b) = RT$$

Now,

$$\text{Dimension of } p = \text{Dimension of } \frac{a}{v^2} \quad \text{--- (I)}$$

$$\text{Dimension of } v = \text{Dimension of } b \quad \text{--- (II)}$$

From (I),

$$\text{Dimension of } v^2 [a]$$

$$= \frac{[M^1 L^{-1} T^{-2}]}{[M^1 L^5 T^{-2}]} \times [L^5]^2$$

$$\text{unit of } a = \text{unit of } p \times \text{unit of } v^2$$

$$= \frac{N}{m^2} \times m^6$$

$$= Nm^4$$

$$\text{From (ii), } [b] = [V] = [M^0 L^3 T^0]$$

$$\therefore \text{unit of } b = \text{unit of } V = m^3$$

$$\therefore [ab] = [M^1 L^5 T^{-2}] [M^0 L^3 T^0]$$

(c) (i) 3

(ii) 3

(iii) 4

(iv) 1

d) Given,

$$A = \frac{a^2 b^3}{c \sqrt{a}}$$

$$\therefore \frac{\Delta a}{a} \times 100 = 1\% \quad , \quad \frac{\Delta c}{c} \times 100 = 2\%$$

$$\frac{\Delta b}{b} \times 100 = 3\% \quad , \quad \frac{\Delta d}{d} \times 100 = 2\%$$

$$\begin{aligned} \therefore \frac{\Delta A}{A} \times 100 &= 2 \frac{\Delta a}{a} \times 100 + 3 \frac{\Delta b}{b} \times 100 + \\ &\frac{\Delta c}{c} \times 100 + \frac{1}{2} \times \frac{\Delta d}{d} \times 100 \\ &= 2 \times 1 + 3 \times 3 + 2 + \frac{1}{2} \times 2 \\ &= 2 + 9 + 2 + 1 \\ &= 14\% \end{aligned}$$

Q.3 (a) Let,

$$\eta \propto l^a T^b m^c$$

where,

$$[l] = M^0 L^1 T^0$$

$$[T] = M^1 L^1 T^{-2} \text{ (force)}$$

$$[m] = M^1 L^{-1} T^0$$

Now,

$$[M^0 L^0 T^{-1}] = [M^0 L^1 T^0]^a [M^1 L^1 T^{-2}]^b [M^1 L^{-1} T^0]^c$$

$$[M^0 L^0 T^{-1}] = [M^0 L^a T^0] [M^b L^b T^{-2b}] [M^c L^{-c} T^0]$$

Then,

$$b + c = 0 \quad \text{--- (i)}$$

$$a + b - c = 0 \quad \text{--- (ii)}$$

$$-2b = -1 \quad \text{--- (iii)}$$

$$\therefore b = \frac{1}{2}$$

$$\therefore c = -\frac{1}{2}$$

$$a = 1$$

$$\therefore \eta \propto \frac{1}{l} \sqrt{T/m}$$

*) Average length

$$= \frac{2.48 + 2.46 + 2.49 + 2.50 + 2.52 + 2.43}{6}$$
$$= \frac{14.88}{6} = 2.48 \text{ m}$$

Mean absolute error

Now, #

$$\Delta l_1 = \cancel{\Delta l} \cdot 2.48 - 2.48 = 0 \text{ m}$$

$$\Delta l_2 = 2.48 - 2.46 = 0.02 \text{ m}$$

$$\Delta l_3 = 2.48 - 2.49 = -0.01 \text{ m}$$

$$\Delta l_4 = 2.48 - 2.50 = -0.02 \text{ m}$$

$$\Delta l_5 = 2.48 - 2.52 = -0.04 \text{ m}$$

$$\Delta l_6 = 2.48 - 2.43 = 0.05 \text{ m}$$

Now,

mean absolute error

$$= \frac{|0| + |0.02| + |-0.01| + |-0.02| + |-0.04| + |0.05|}{6}$$

$$= \frac{0 + 0.02 + 0.01 + 0.02 + 0.04 + 0.05}{6}$$

$$= \frac{0.14}{6} = 0.023 \text{ m}$$

$$\% \text{ error} = \frac{0.02}{2.48} \times 100$$

$$= 0.008 \times 100 = 0.8\%$$

$$\therefore \text{Length} = (2.48 \pm 0.02) \text{ m}$$

(c) Parallax angle is the angle made between great circle passing the two lines of sight of a distant planet or a star from the two observation from the surface of the earth.

$$\begin{aligned} \phi &= 2^\circ 36' = 156' = (156 \times 60)'' \\ &= 156 \times 60 \times 4.85 \times 10^{-6} \\ &= 45,396 \times 10^{-6} \\ &= 45.396 \times 10^{-2} \text{ m} \end{aligned}$$

$$\begin{aligned} \text{Also, } d &= 552 \text{ km} \\ &= 552 \times 10^3 \text{ m} \end{aligned}$$

$$\begin{aligned} \therefore D &= \frac{d}{\phi} = \frac{552 \times 10^3}{45.396 \times 10^{-2}} \\ &= 12.15 \times 10^5 \text{ m} \end{aligned}$$

(d) Given,

$$\begin{aligned} T &\propto \rho^a d T \propto \rho^a g^b E^c \\ T &= K \rho^a g^b E^c \quad \text{--- (1)} \end{aligned}$$

$$[T] = [ML^{-1}T^{-2}]^a [ML^{-3}]^b [ML^2T^{-2}]^c$$

So, we get,

$$0 = a + b + c \quad \text{--- (1)}$$

$$\begin{aligned} 0 &= -a - 3b + 2c && \text{--- (iii)} \\ 1 &= -2a - 2c && \text{--- (iv)} \end{aligned}$$

From (iv),

$$a + c = -\frac{1}{2} \quad \text{--- (v)}$$

Inserting it in (iii), we get,

$$0 = b - \frac{1}{2}$$

$$\Rightarrow b = \frac{1}{2}$$

From eqⁿ (5),

$$a = -\frac{1}{2} - c$$

Putting values of a and b in (ii),

$$0 = -\left(-\frac{1}{2} - c\right) - 3 \times \frac{1}{2} + 2c$$

$$0 = +\frac{1}{2} + c - \frac{3}{2} + 2c$$

$$\Rightarrow 3c = 1$$

$$\Rightarrow c = \frac{1}{3}$$

Thus, value of (c) in (5)

$$a + \frac{1}{3} = -\frac{1}{2}$$

$$\Rightarrow a = -\frac{1}{2} - \frac{1}{3}$$

$$\therefore a = -\frac{5}{6}$$

$$\therefore a = -\frac{5}{6}, \quad b = \frac{1}{2} \quad \text{and} \quad c = \frac{1}{3}$$