

Electric Potential: Paper - 01

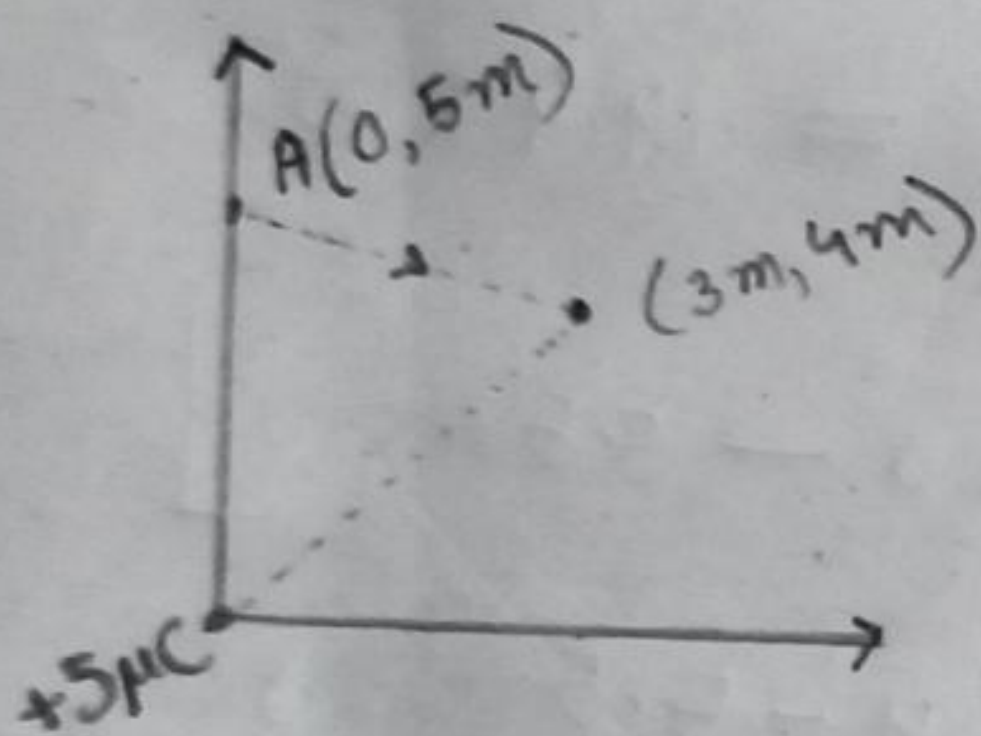
Ans to Q. No - 2

As the displacement and centripetal force are perpendicular to each other therefore work done,

$$W = Fd \cos 90^\circ$$

$$\Rightarrow \boxed{W = 0} //$$

Ans to Q. No - 3



$$\therefore W_{A \rightarrow B} = q_0 (V_B - V_A) \quad \text{--- (i)}$$

Where, $q_0 = 5\mu\text{C} = 5 \times 10^{-6}\text{C}$

Charge of an electron, $q_e = 1.6 \times 10^{-19}\text{C}$

$$V_A = 9 \times 10^9 \times \frac{q}{r_A}$$

$$= 9 \times 10^9 \times \frac{5 \times 10^{-6}}{5}$$

$$= 9 \times 10^3 \text{ V}$$

$$V_B = 9 \times 10^9 \times \frac{q}{r_B}$$

$$= 9 \times 10^9 \times \frac{5 \times 10^{-6}}{5}$$

$$= 9 \times 10^3 \text{ V}$$

$$\therefore W_{A \rightarrow B} = q_0 (V_B - V_A)$$

$$= 1.6 \times 10^{-19} (9 \times 10^3 - 9 \times 10^3)$$

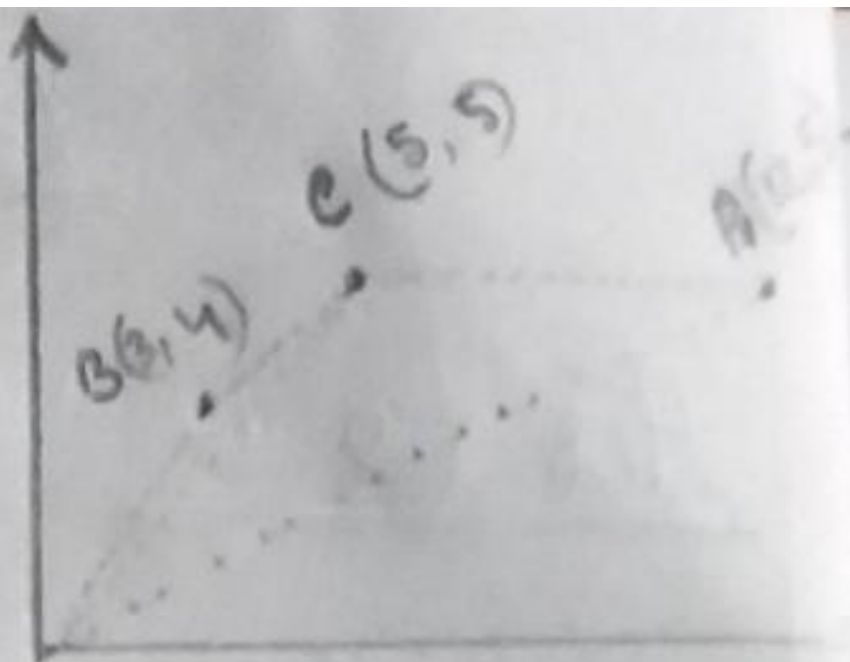
$$= 0$$

\therefore The work done is 0.

Ans to Q No. 4

Here, $q = 8 \mu\text{C} = 8 \times 10^{-6} \text{C}$

$q_0 = -2 \text{ nC} = -2 \times 10^{-9} \text{C}$



$A \rightarrow (12\text{m}, 5\text{m})$; $B \rightarrow (3\text{m}, 4\text{m})$; $C \rightarrow (5\text{m}, 5\text{m})$

$\therefore W_{A \rightarrow B} = q_0 [V_B - V_A]$ — (i)

$V_A = 9 \times 10^9 \frac{q}{r_A}$

$= 9 \times 10^9 \frac{8 \times 10^{-6}}{13}$

$= 5.53 \times 10^3$

$V_B = 9 \times 10^9 \frac{q}{r_B}$

$= 9 \times 10^9 \frac{8 \times 10^{-6}}{5}$

$= 14.4 \times 10^3$

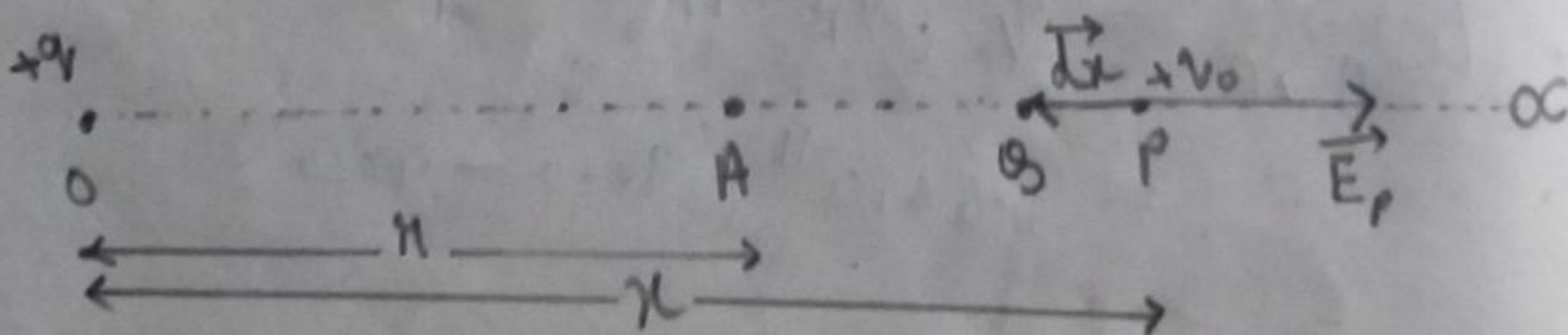
(i) $\rightarrow W_{A \rightarrow B} = -2 \times 10^{-9} [14.4 \times 10^3 - 5.53 \times 10^3]$

$= -2 \times 10^{-9} [14.4 - 5.53] \times 10^3$

$= -17.74 \times 10^{-7}$

$= -1.77 \times 10^{-6} \text{ J}$

Ans to Q No-5



Let a point charge $+q$ be at O due to which we have to find out electric potential at A .

By defⁿ of electric potential at A:—

$$V_A = \frac{W_{\alpha \rightarrow A}}{q_0} \quad \left[\text{where } W_{\alpha \rightarrow A} \text{ is the amt. of work done in bringing a test charge } +q_0 \text{ from } \alpha \text{ to } A \right]$$

Let $OP = r$ ($r < r < \alpha$)

$$\therefore E_p = \frac{1}{4\pi\epsilon_0} \frac{q}{r^2}$$

Let $\vec{PQ} = d\vec{r}$ (\because P and Q are very much close to each other)

Small amount of work is done in bringing a test charge $+q_0$ from P to Q

$$dW_{P \rightarrow Q} = \vec{F} \cdot \vec{PQ} = \vec{F} \cdot d\vec{r} = q_0 \vec{E}_p \cdot d\vec{r} = q_0 E_p dr$$

$$\Rightarrow dW_{P \rightarrow Q} = q_0 \times \frac{1}{4\pi\epsilon_0} \frac{q}{r^2} dr$$

$$\Rightarrow dW_{P \rightarrow Q} = q_0 E_p dr \cos 180^\circ \quad (\because \vec{E}_p \text{ and } d\vec{r} \text{ are in opp. dirⁿ})$$

$$\Rightarrow dW_{P \rightarrow Q} = -q_0 E_p dr$$

$$\Rightarrow dW_{P \rightarrow Q} = -q_0 \frac{1}{4\pi\epsilon_0} \frac{q}{r^2} dr = -\frac{1}{4\pi\epsilon_0} \frac{q q_0 dr}{r^2}$$

$$\therefore W_{\alpha \rightarrow A} = \int dW_{P \rightarrow Q} = \int_{\alpha}^r -\frac{1}{4\pi\epsilon_0} \frac{q q_0}{r^2} dr = -\frac{q q_0}{4\pi\epsilon_0} \left(\frac{dr}{r^2} \right)$$

$$= -\frac{q q_0}{4\pi\epsilon_0} \left[-\frac{1}{r} \right]_{\alpha}^r$$

$$\Rightarrow \frac{W_{\alpha \rightarrow A}}{q_0} = +\frac{q}{4\pi\epsilon_0} \left[\frac{1}{r} - \frac{1}{\alpha} \right]$$

$$\Rightarrow \boxed{V_A = \frac{1}{4\pi\epsilon_0} \frac{q}{r}}$$